

# *Deep Learning: Theory and Practice*

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## Recurrent Neural Networks

28-03-2019

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# Introduction

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- ❖ The standard DNN / CNN paradigms
  - ❖  $(\mathbf{x}, \mathbf{y})$  - ordered pair of data vectors / images ( $\mathbf{x}$ ) and target ( $\mathbf{y}$ )
- ❖ Moving to sequence data
  - ❖  $(\mathbf{x}(t), \mathbf{y}(t))$  where this could be sequence to sequence mapping task.
  - ❖  $(\mathbf{x}(t), \mathbf{y})$  where this could be a sequence to vector mapping task.



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# Introduction

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- ❖ Difference between CNNs / DNNs
  - ❖  $(x(t), y(t))$  where this could be sequence to sequence mapping task.
    - ❖ Input features / output targets are correlated in time.
    - ❖ Unlike standard models where each pair is independent.
    - ❖ Need to model dependencies in the sequence over time.



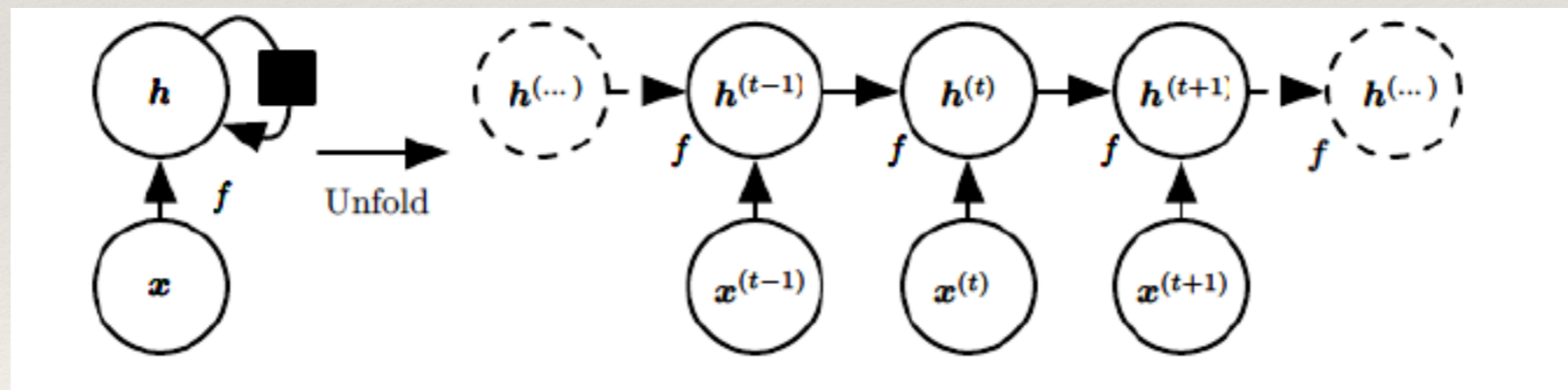
# Introduction to Recurrent Networks

$$\mathbf{s}^{(t)} = f(\mathbf{s}^{(t-1)}; \boldsymbol{\theta}),$$

$$\begin{aligned}\mathbf{s}^{(3)} &= f(\mathbf{s}^{(2)}; \boldsymbol{\theta}) \\ &= f(f(\mathbf{s}^{(1)}; \boldsymbol{\theta}); \boldsymbol{\theta})\end{aligned}$$

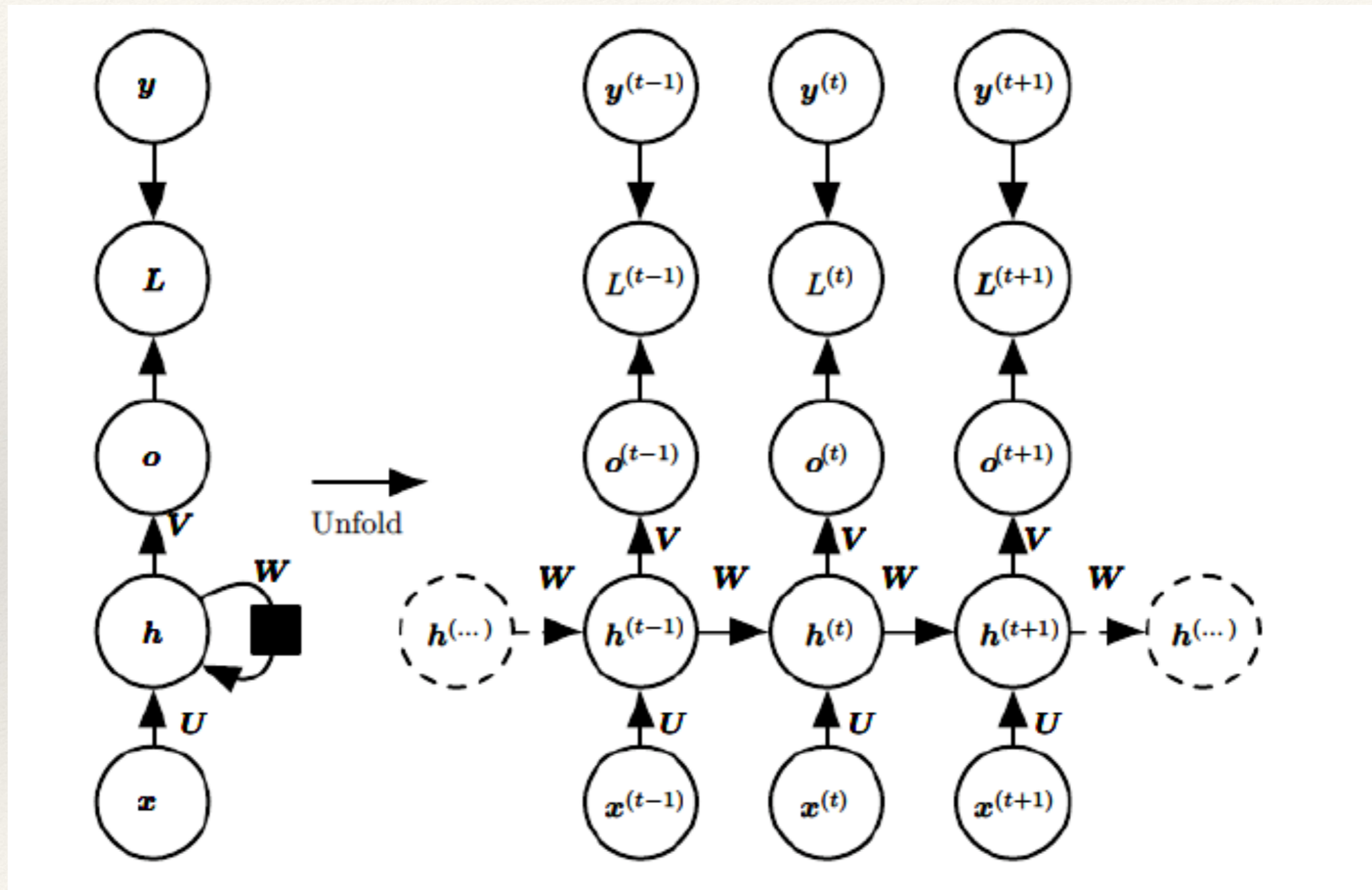
$$\mathbf{s}^{(t)} = f(\mathbf{s}^{(t-1)}, \mathbf{x}^{(t)}; \boldsymbol{\theta}),$$

$$\mathbf{h}^{(t)} = f(\mathbf{h}^{(t-1)}, \mathbf{x}^{(t)}; \boldsymbol{\theta}),$$



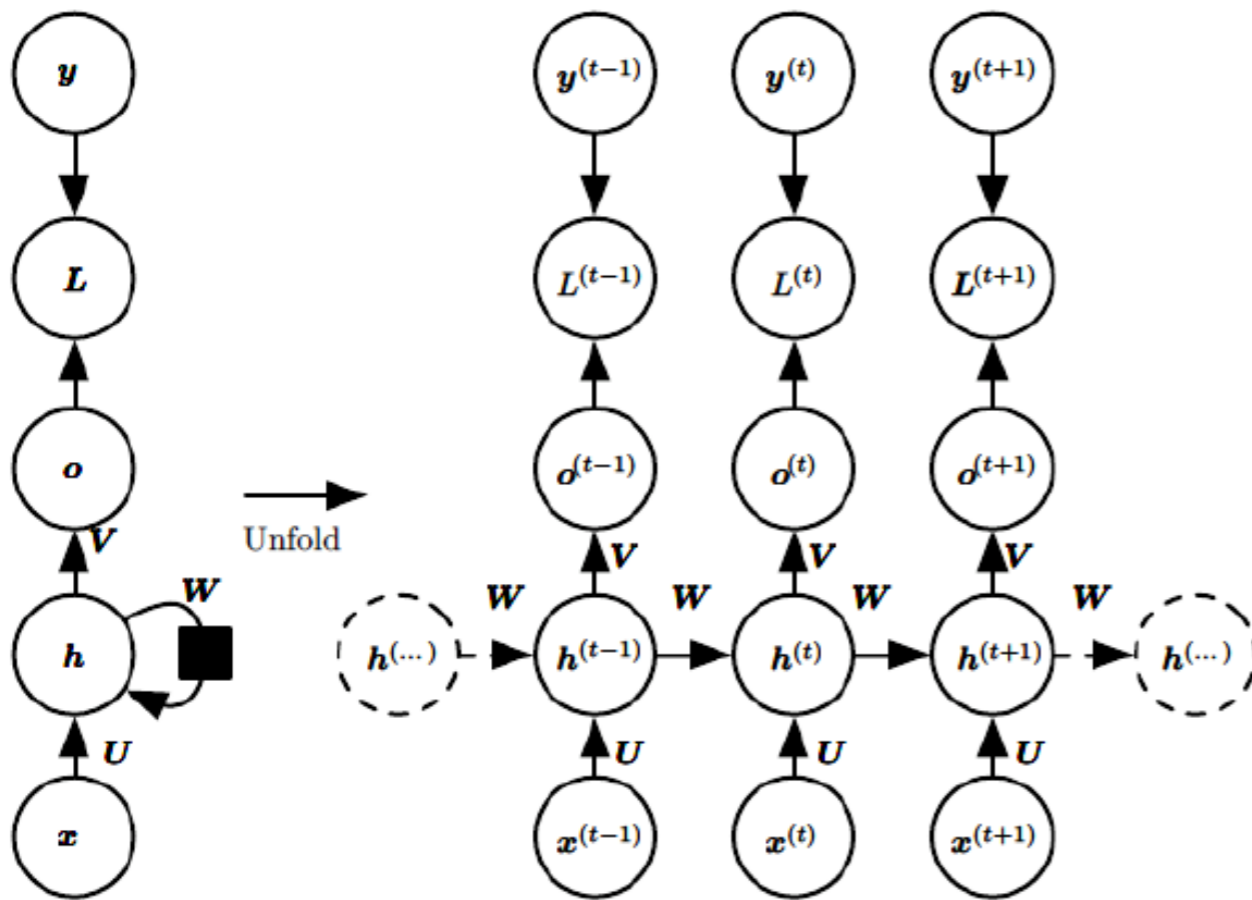


# Recurrent Networks





# Recurrent Networks



$$\begin{aligned} \mathbf{a}^{(t)} &= \mathbf{b} + \mathbf{W}\mathbf{h}^{(t-1)} + \mathbf{U}\mathbf{x}^{(t)} \\ \mathbf{h}^{(t)} &= \tanh(\mathbf{a}^{(t)}) \\ \mathbf{o}^{(t)} &= \mathbf{c} + \mathbf{V}\mathbf{h}^{(t)} \\ \hat{\mathbf{y}}^{(t)} &= \text{softmax}(\mathbf{o}^{(t)}) \end{aligned}$$

$$\begin{aligned} &L(\{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(\tau)}\}, \{\mathbf{y}^{(1)}, \dots, \mathbf{y}^{(\tau)}\}) \\ &= \sum_t L^{(t)} \\ &= - \sum_t \log p_{\text{model}}(y^{(t)} | \{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(t)}\}) \end{aligned}$$



# Back Propagation in RNNs

$$\begin{aligned} \mathbf{a}^{(t)} &= \mathbf{b} + \mathbf{W}\mathbf{h}^{(t-1)} + \mathbf{U}\mathbf{x}^{(t)} \\ \mathbf{h}^{(t)} &= \tanh(\mathbf{a}^{(t)}) \\ \mathbf{o}^{(t)} &= \mathbf{c} + \mathbf{V}\mathbf{h}^{(t)} \\ \hat{\mathbf{y}}^{(t)} &= \text{softmax}(\mathbf{o}^{(t)}) \end{aligned}$$

## Model Parameters

$$\mathbf{U}, \mathbf{V}, \mathbf{W}, \mathbf{b} \text{ and } \mathbf{c}$$

## Gradient Descent

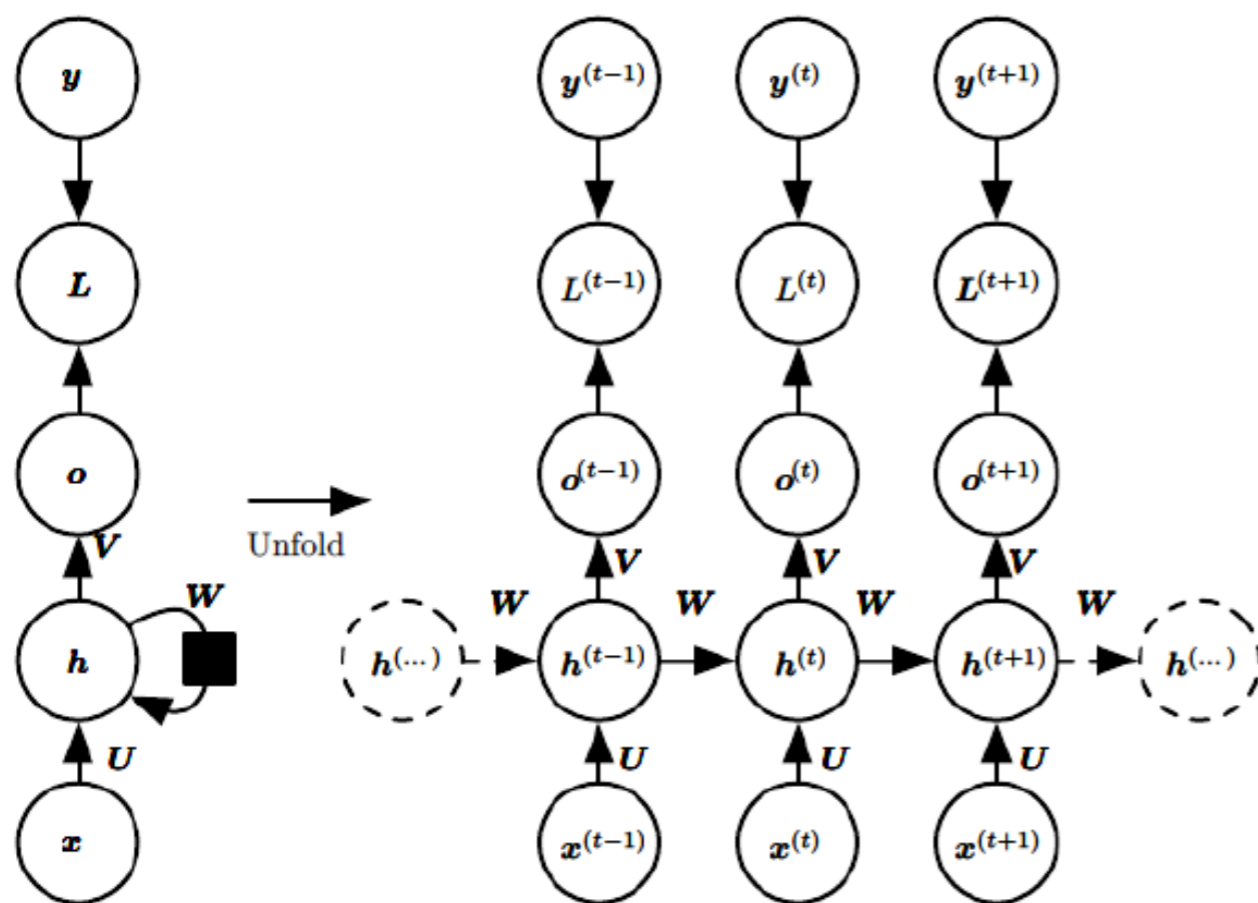
$$\begin{aligned} &L(\{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(\tau)}\}, \{\mathbf{y}^{(1)}, \dots, \mathbf{y}^{(\tau)}\}) \\ &= \sum_t L^{(t)} \\ &= - \sum_t \log p_{\text{model}}(y^{(t)} | \{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(t)}\}) \end{aligned}$$

$$\frac{\partial L}{\partial L^{(t)}} = 1.$$

$$(\nabla_{\boldsymbol{\alpha}^{(t)}} L)_i = \frac{\partial L}{\partial o_i^{(t)}} = \frac{\partial L}{\partial L^{(t)}} \frac{\partial L^{(t)}}{\partial o_i^{(t)}} = \hat{y}_i^{(t)} - \mathbf{1}_{i, y^{(t)}}$$



# Recurrent Networks



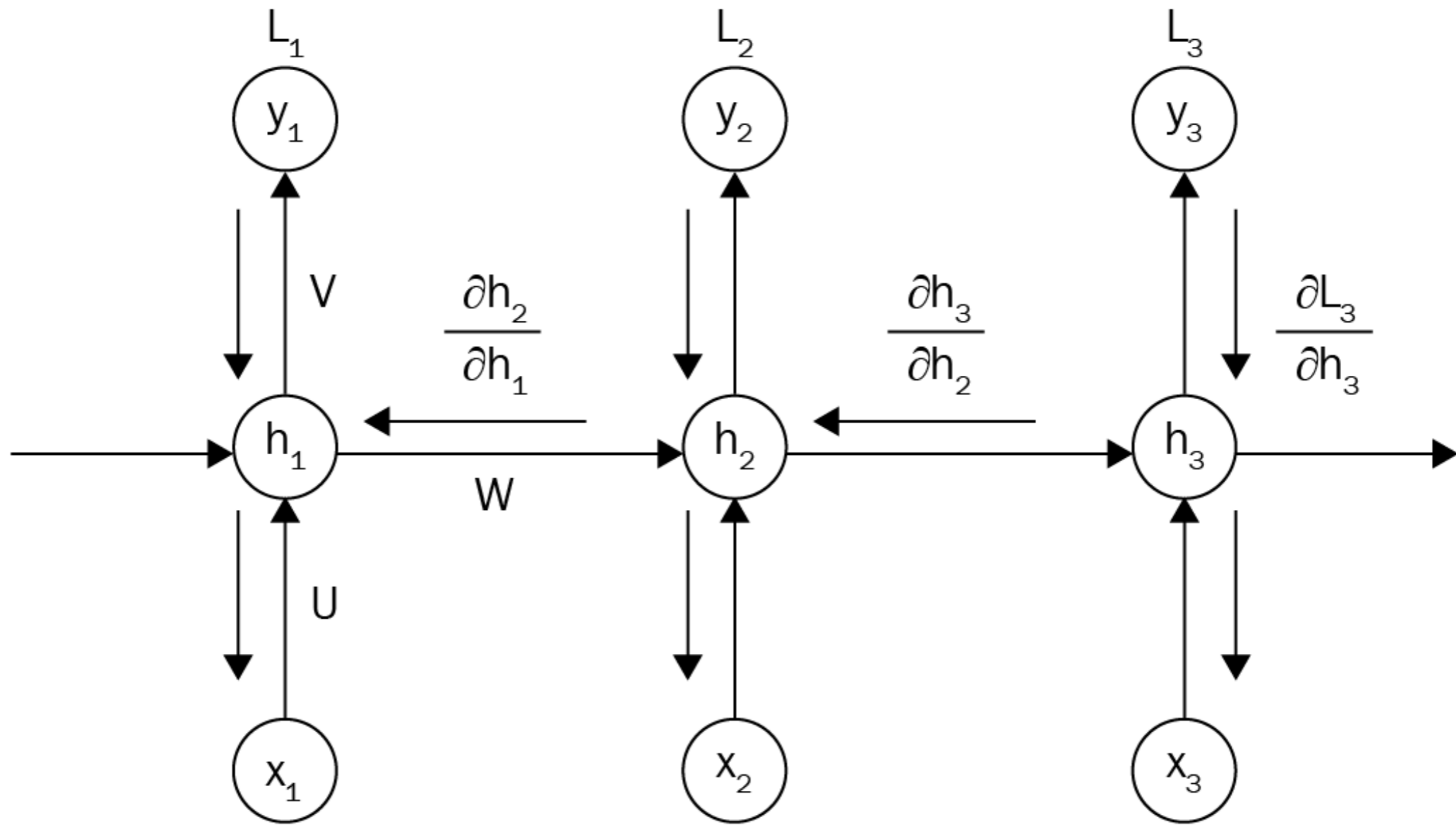
$$(\nabla_{\mathbf{o}^{(t)}} L)_i = \frac{\partial L}{\partial o_i^{(t)}} = \frac{\partial L}{\partial L^{(t)}} \frac{\partial L^{(t)}}{\partial o_i^{(t)}} = \hat{y}_i^{(t)} - \mathbf{1}_{i,y^{(t)}}$$

$$\nabla_{\mathbf{h}^{(\tau)}} L = \mathbf{V}^\top \nabla_{\mathbf{o}^{(\tau)}} L.$$

$$\begin{aligned} \nabla_{\mathbf{h}^{(t)}} L &= \left( \frac{\partial \mathbf{h}^{(t+1)}}{\partial \mathbf{h}^{(t)}} \right)^\top (\nabla_{\mathbf{h}^{(t+1)}} L) + \left( \frac{\partial \mathbf{o}^{(t)}}{\partial \mathbf{h}^{(t)}} \right)^\top (\nabla_{\mathbf{o}^{(t)}} L) \\ &= \mathbf{W}^\top (\nabla_{\mathbf{h}^{(t+1)}} L) \text{diag} \left( 1 - \left( \mathbf{h}^{(t+1)} \right)^2 \right) + \mathbf{V}^\top (\nabla_{\mathbf{o}^{(t)}} L) \end{aligned}$$

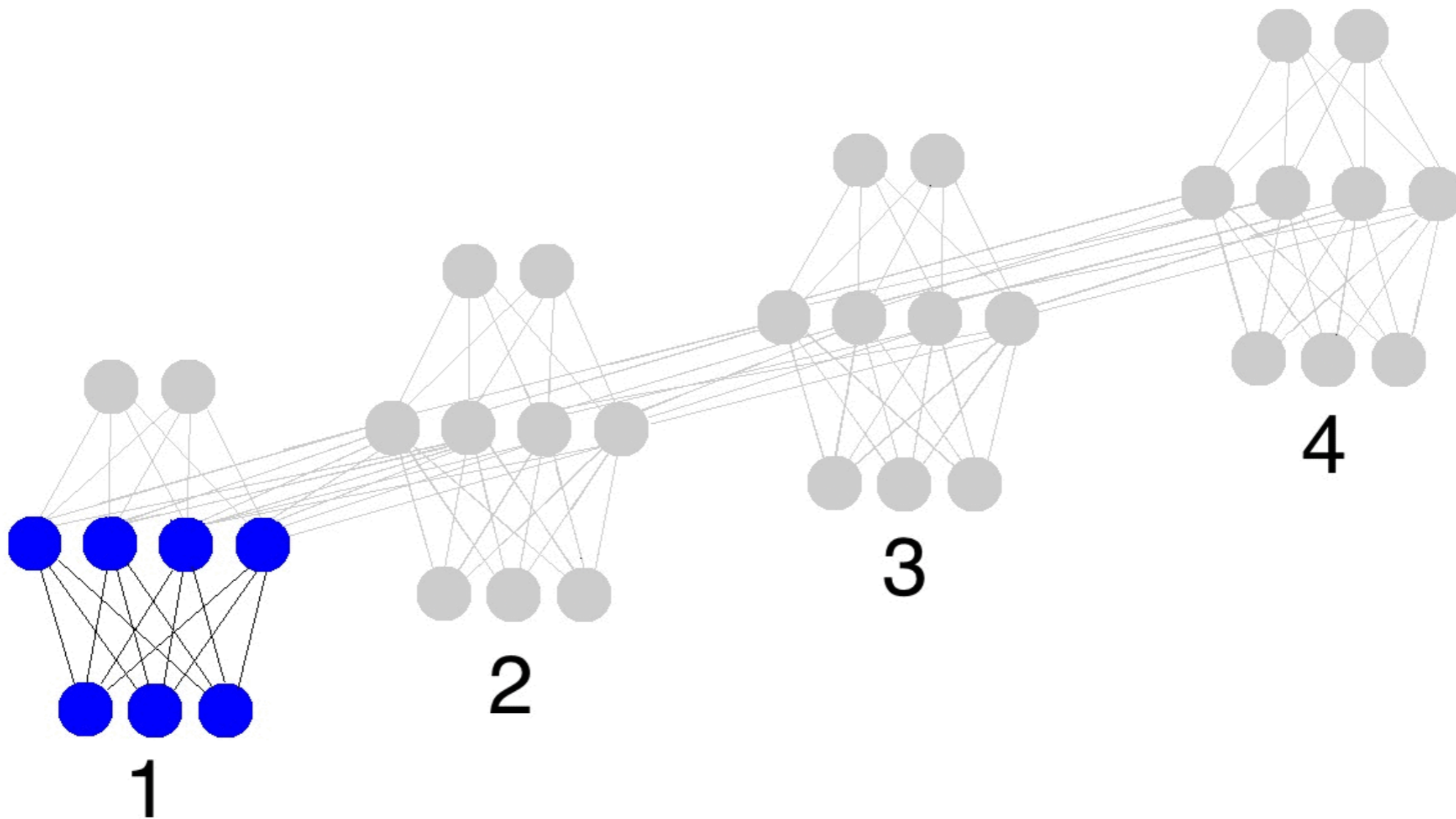


# Back Propagation Through Time



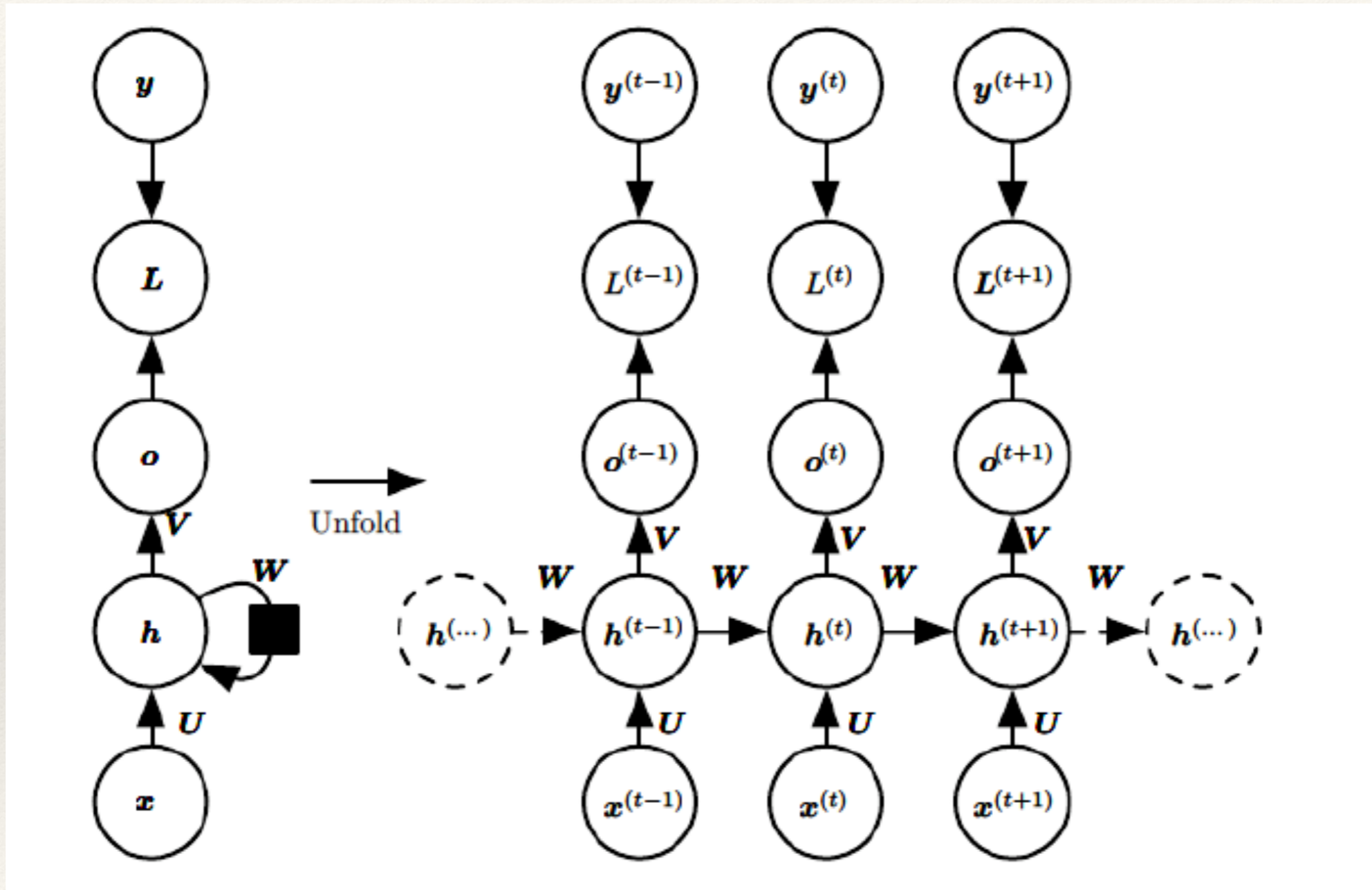


# Back Propagation Through Time



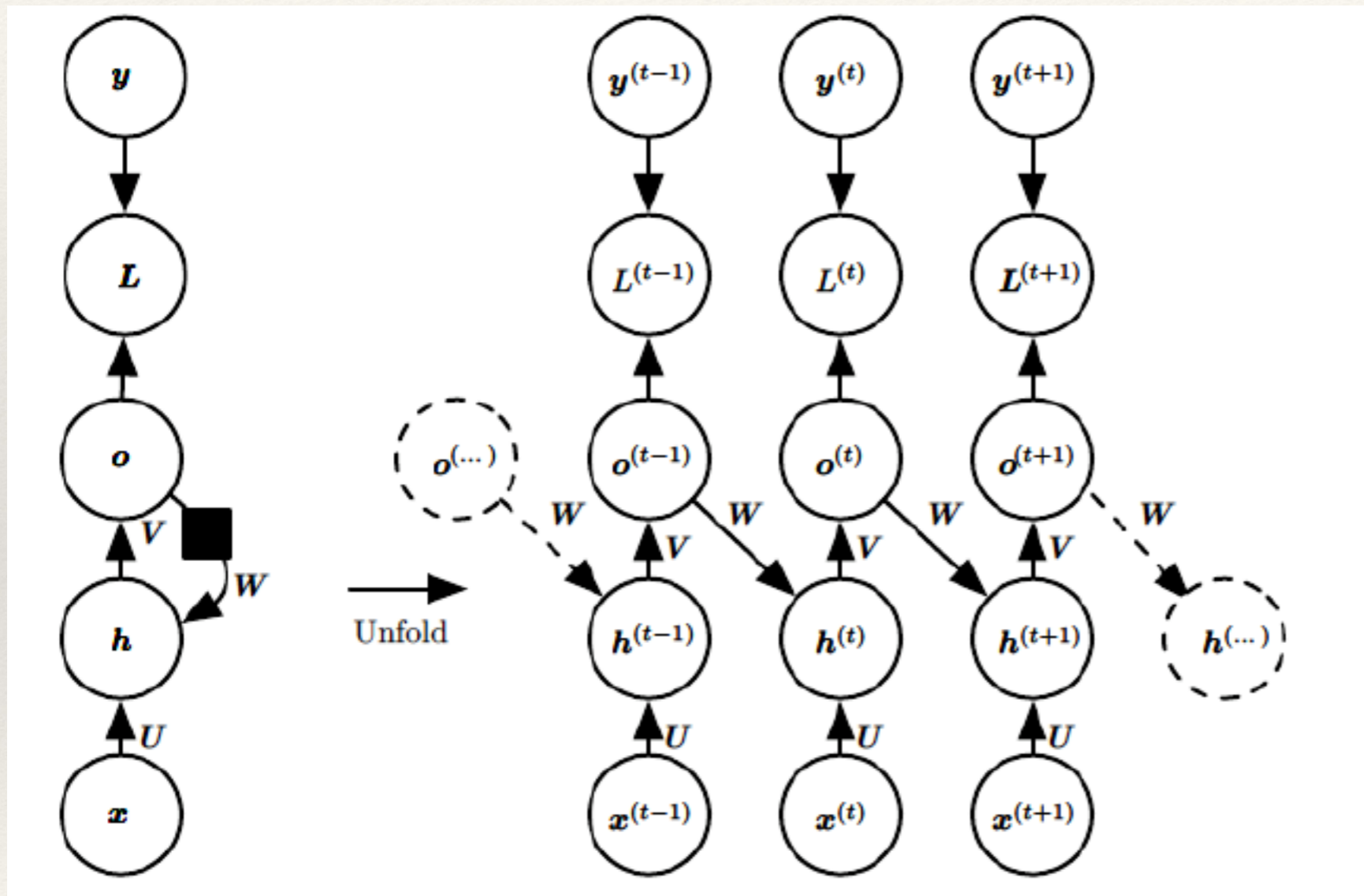


# Standard Recurrent Networks





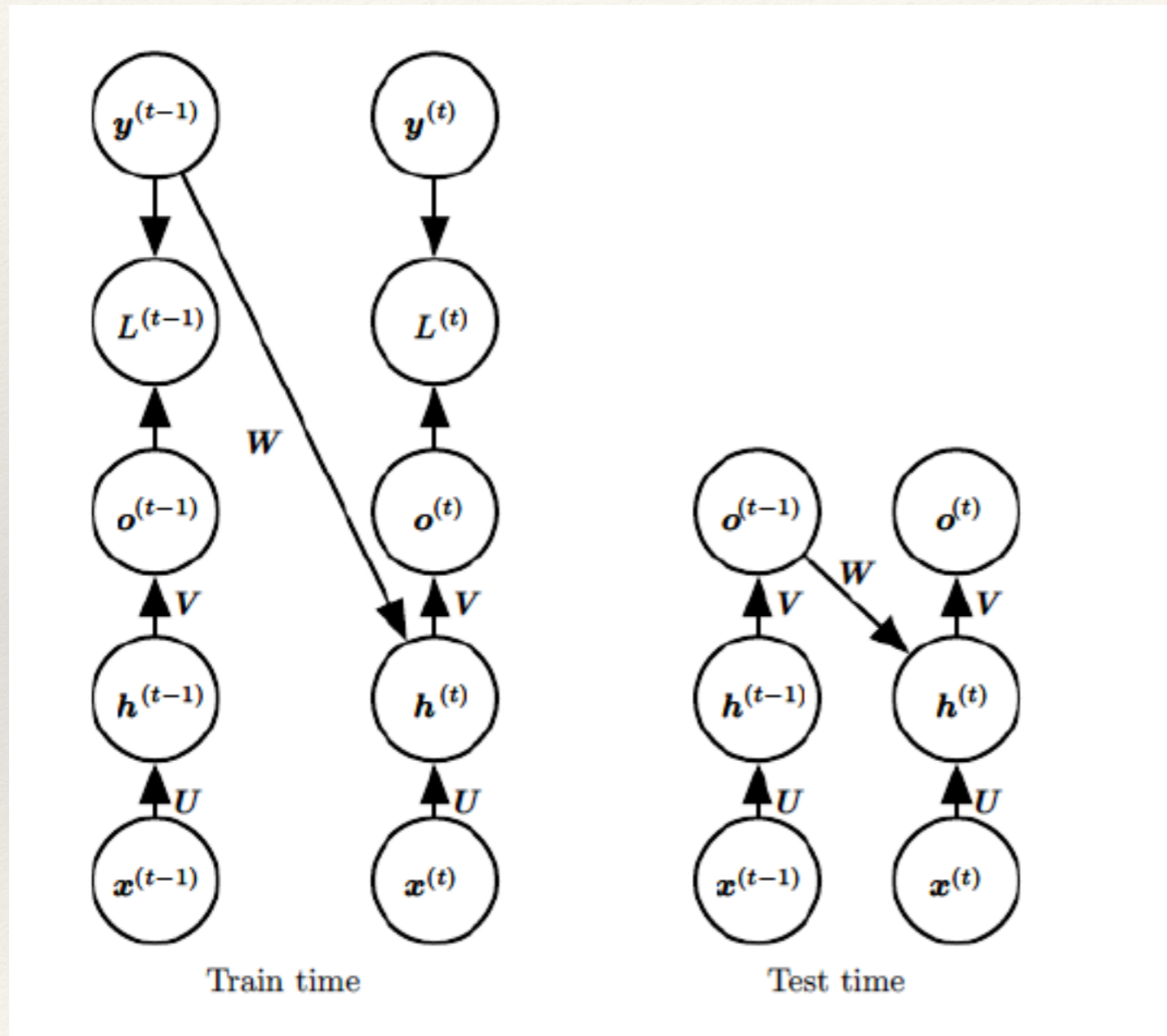
# Other Recurrent Networks



**Teacher  
Forcing Networks**



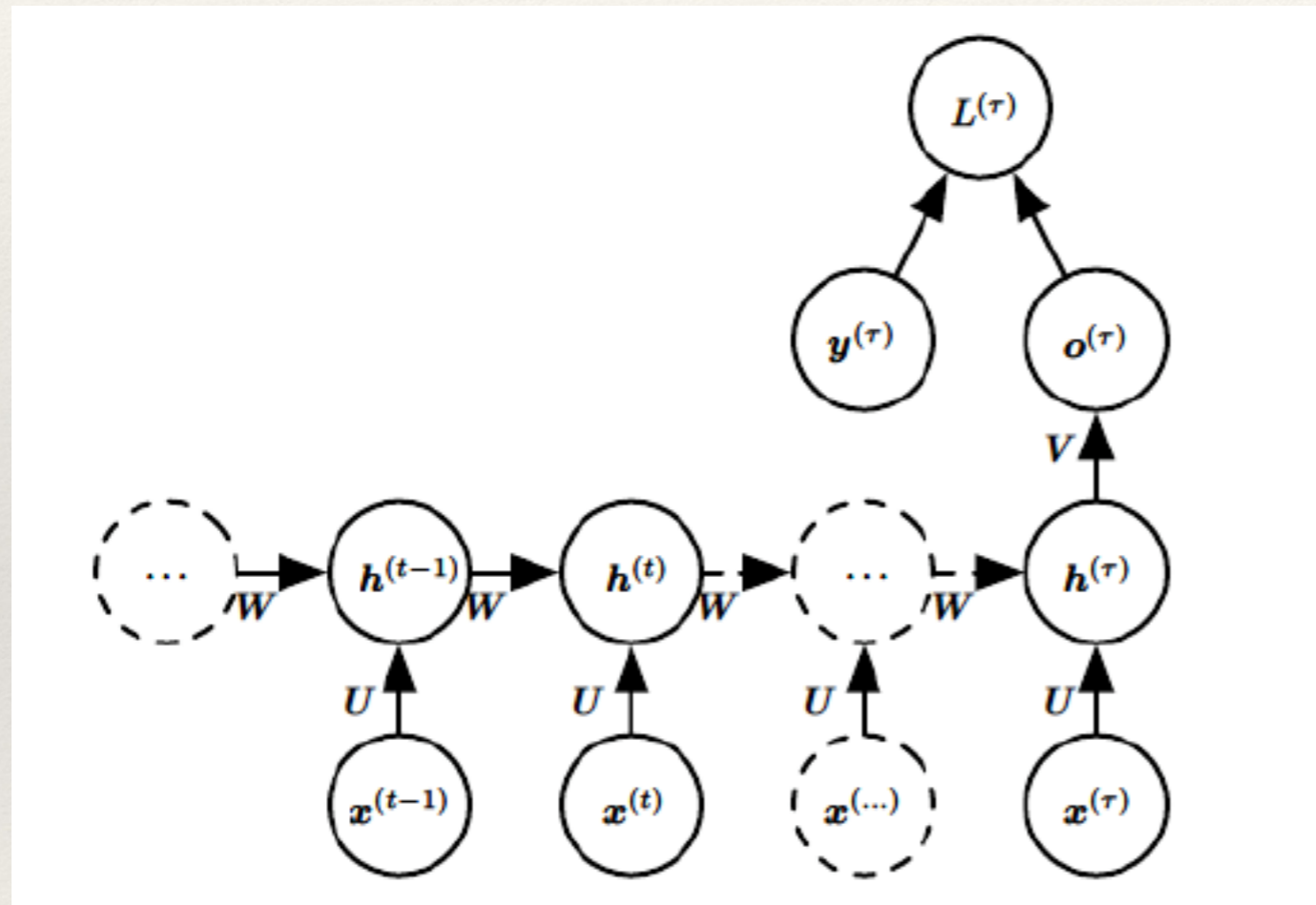
# Recurrent Networks



**Teacher  
Forcing Networks**



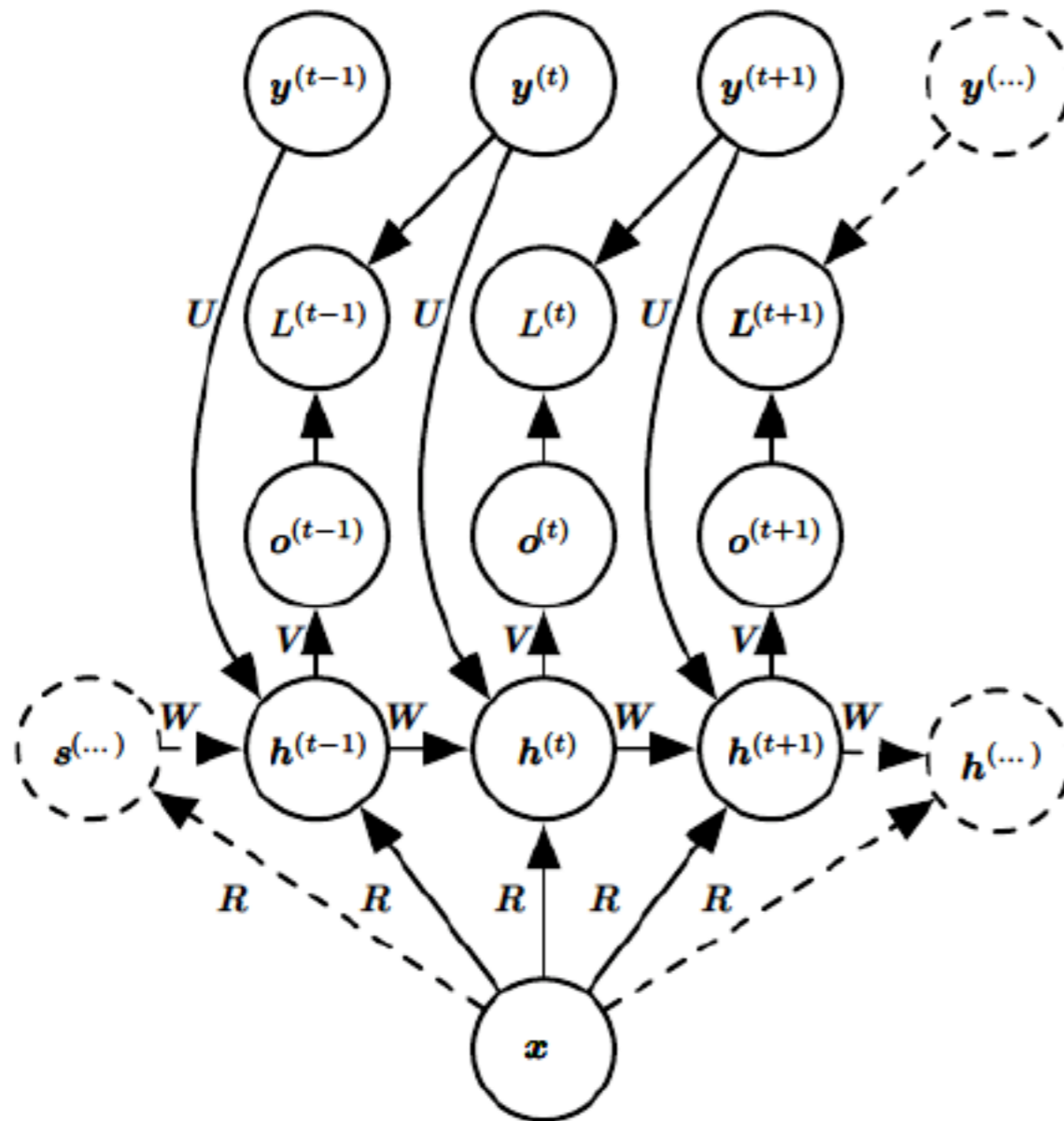
# Recurrent Networks



**Multiple Input  
Single Output**



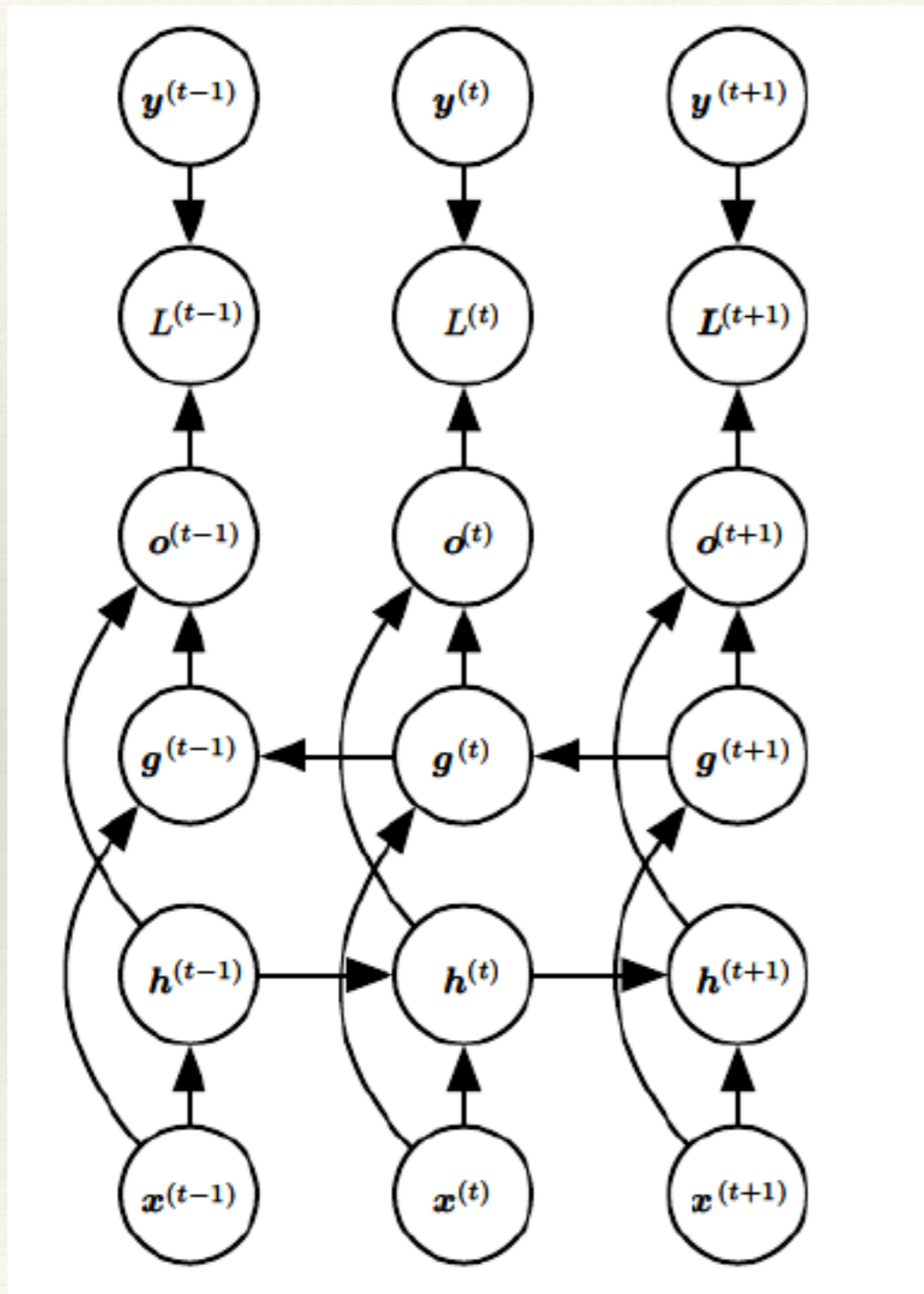
# Recurrent Networks



**Single Input  
Multiple Output**



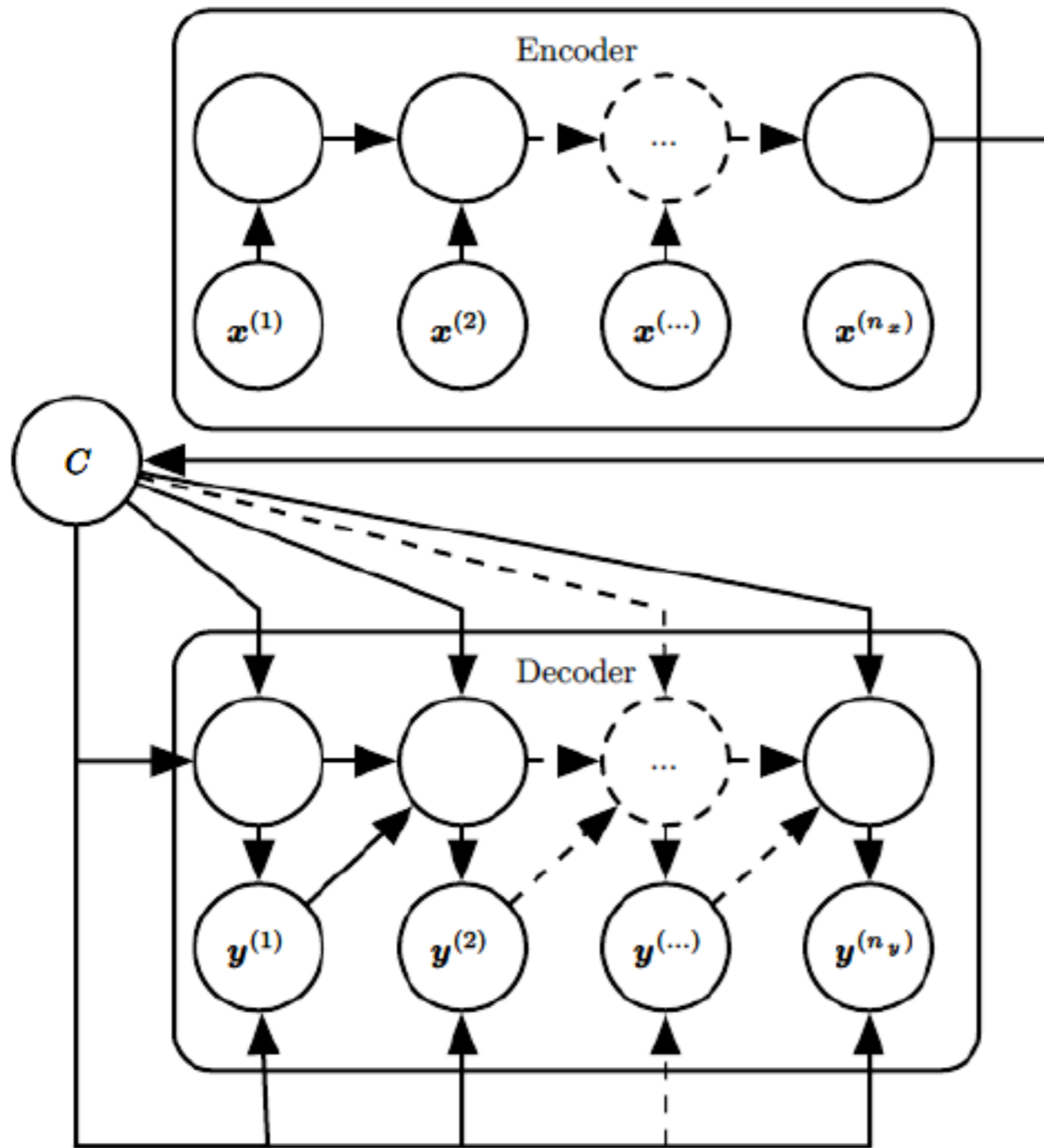
# Recurrent Networks



**Bi-directional  
Networks**



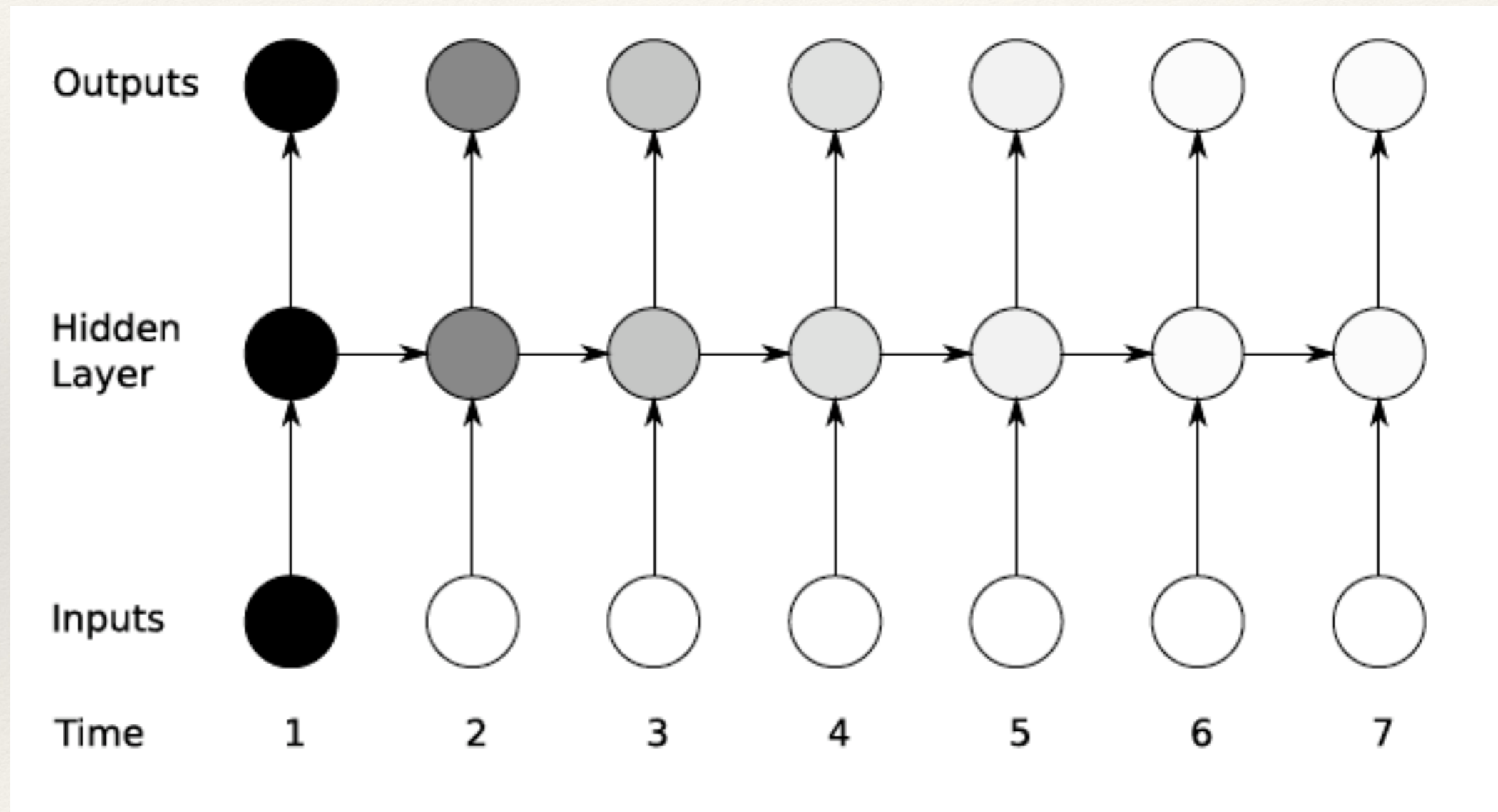
# Recurrent Networks



**Sequence to  
Sequence  
Mapping Networks**



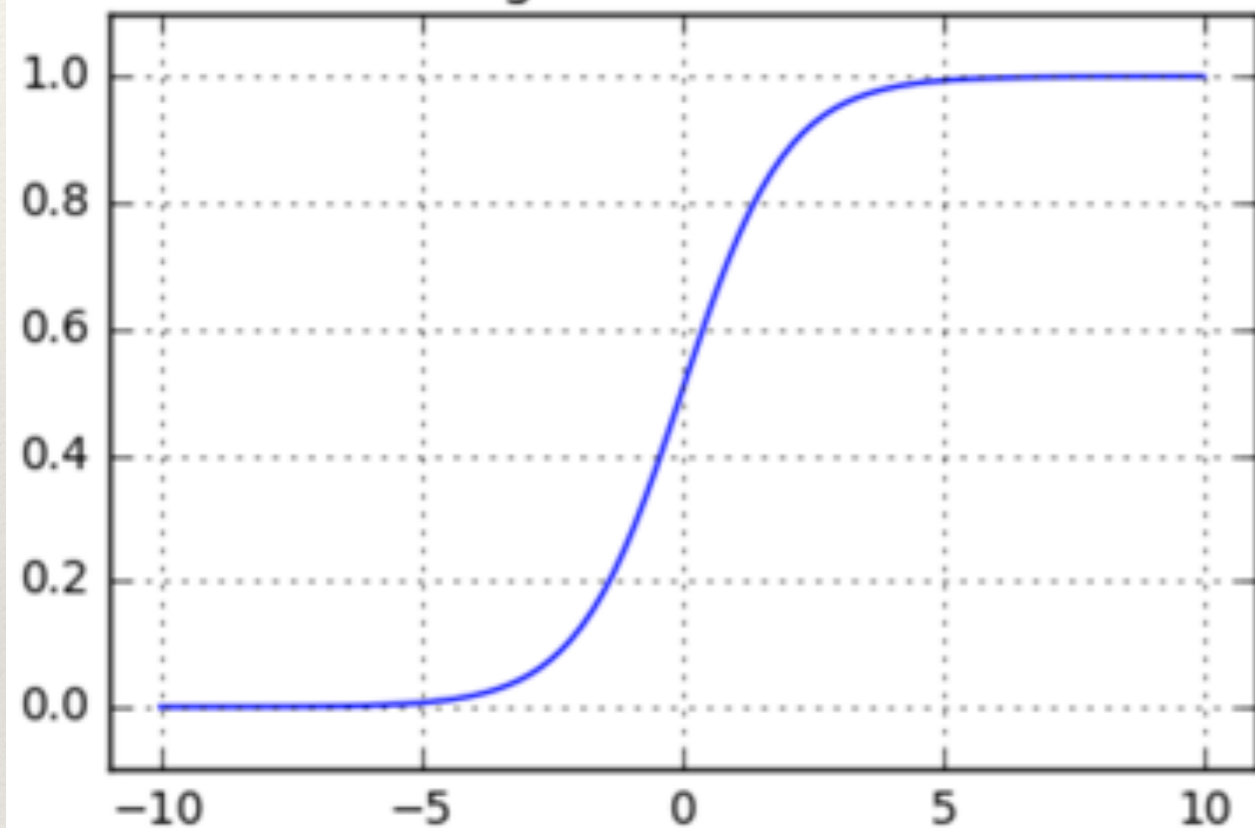
# Long-term Dependency Issues



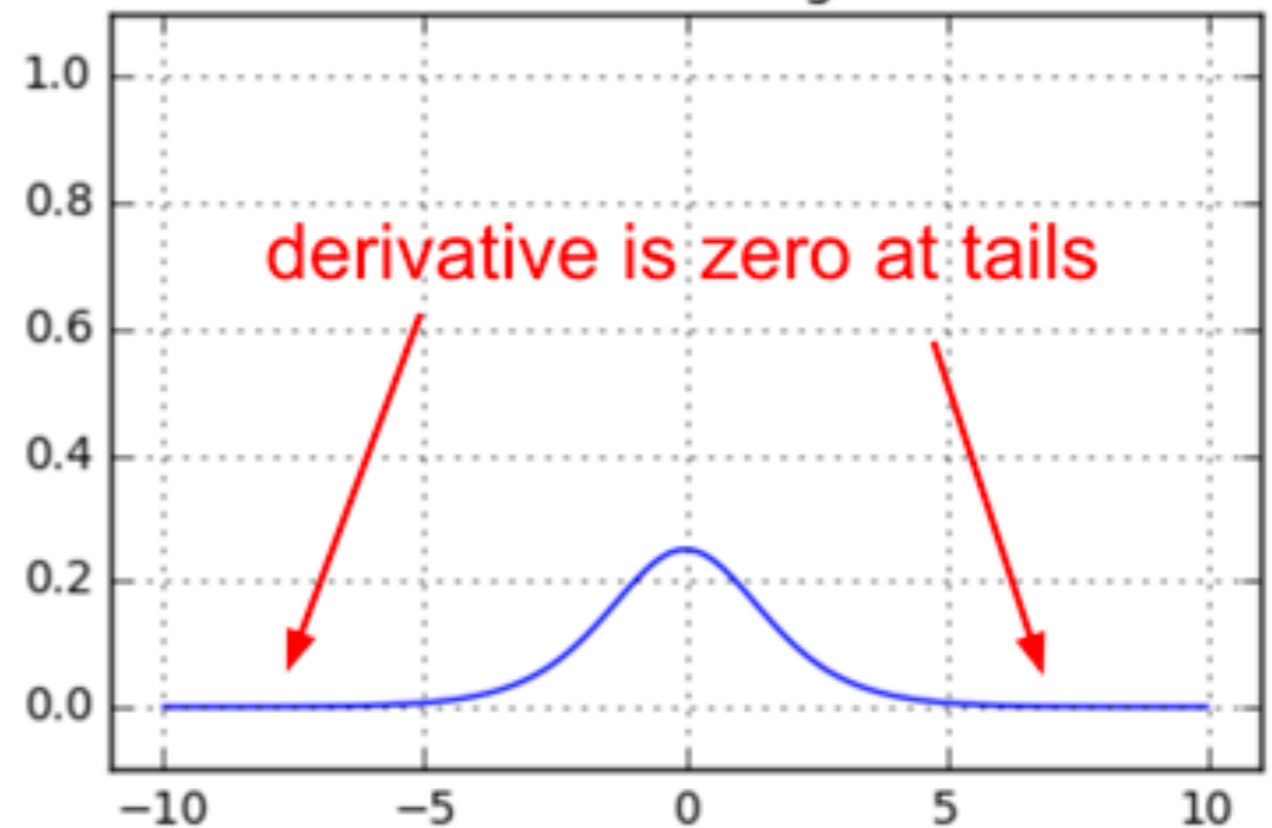


# Vanishing/Exploding Gradients

sigmoid function



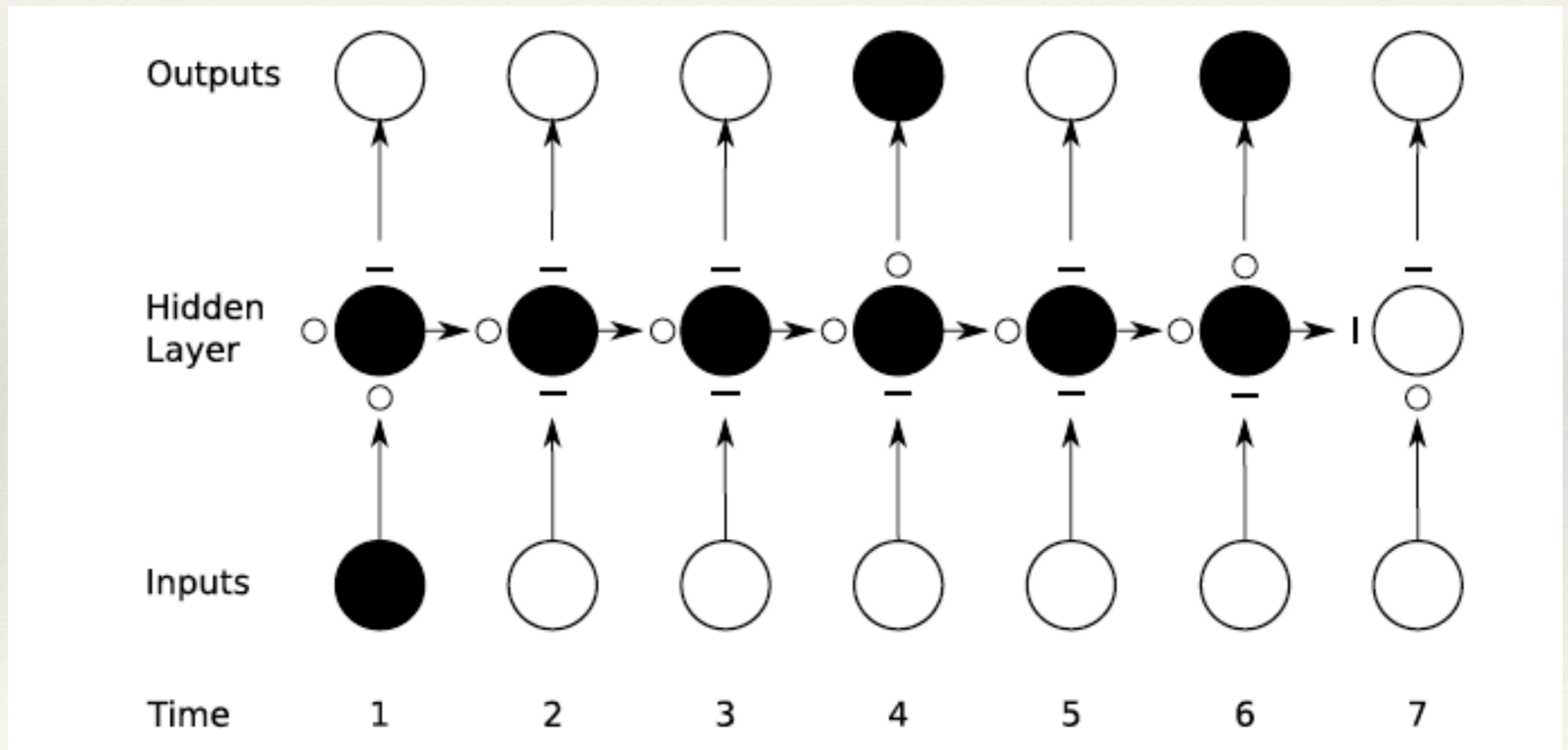
derivative of sigmoid



- ❖ Gradients either vanish or explode
- ❖ Initial frames may not contribute to gradient computations or may contribute too much.



# Long-Short Term Memory





# LSTM Cell

**f** - sigmoid function  
**g, h** - tanh function

## Input Gate

$$a_{\iota}^t = \sum_{i=1}^I w_{i\iota} x_i^t + \sum_{h=1}^H w_{h\iota} b_h^{t-1} + \sum_{c=1}^C w_{c\iota} s_c^{t-1}$$
$$b_{\iota}^t = f(a_{\iota}^t)$$

## Forget Gate

$$a_{\phi}^t = \sum_{i=1}^I w_{i\phi} x_i^t + \sum_{h=1}^H w_{h\phi} b_h^{t-1} + \sum_{c=1}^C w_{c\phi} s_c^{t-1}$$
$$b_{\phi}^t = f(a_{\phi}^t)$$

## Cell

$$a_c^t = \sum_{i=1}^I w_{ic} x_i^t + \sum_{h=1}^H w_{hc} b_h^{t-1}$$
$$s_c^t = b_{\phi}^t s_c^{t-1} + b_{\iota}^t g(a_c^t)$$

## Output Gate

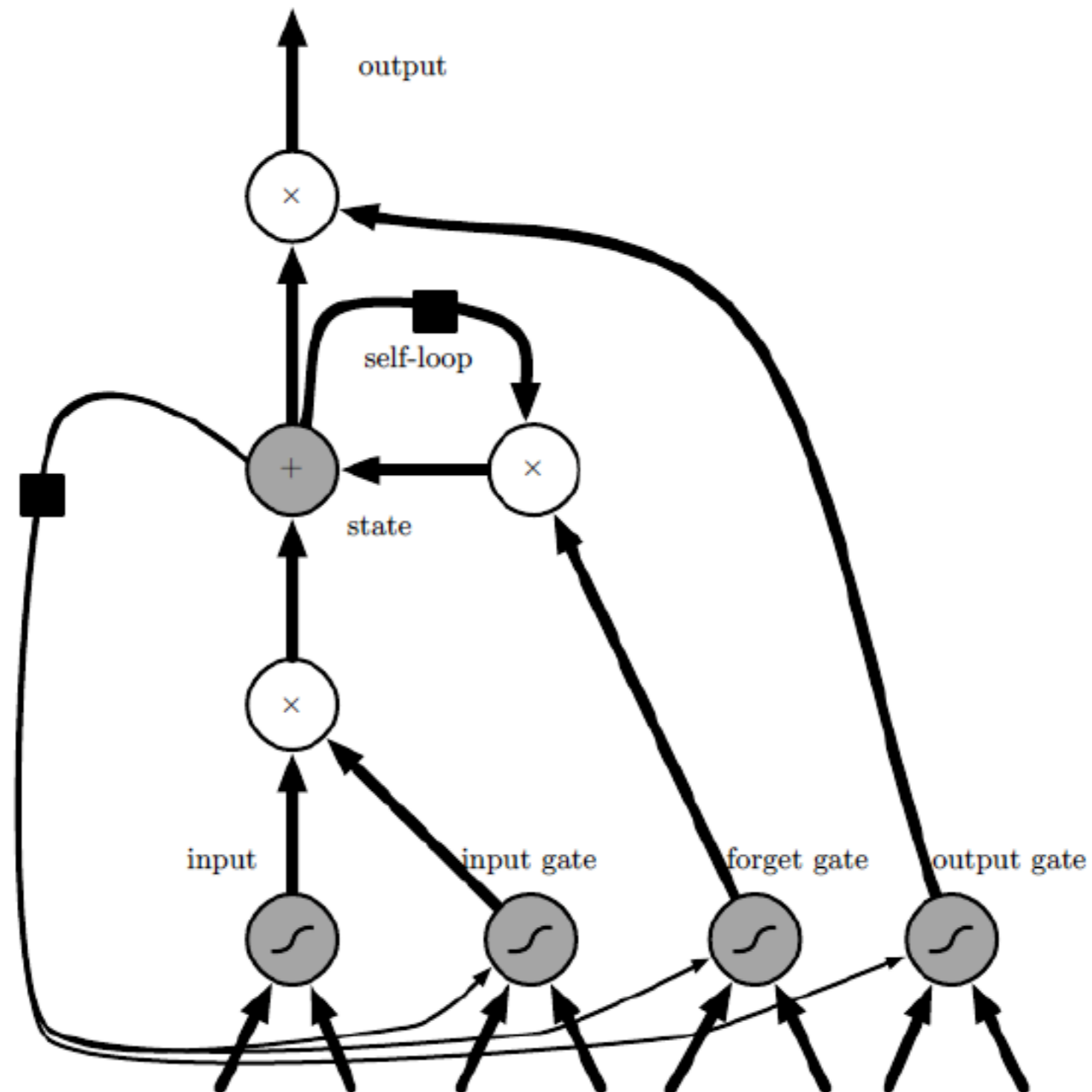
$$a_{\omega}^t = \sum_{i=1}^I w_{i\omega} x_i^t + \sum_{h=1}^H w_{h\omega} b_h^{t-1} + \sum_{c=1}^C w_{c\omega} s_c^t$$
$$b_{\omega}^t = f(a_{\omega}^t)$$

## LSTM output

$$b_c^t = b_{\omega}^t h(s_c^t)$$



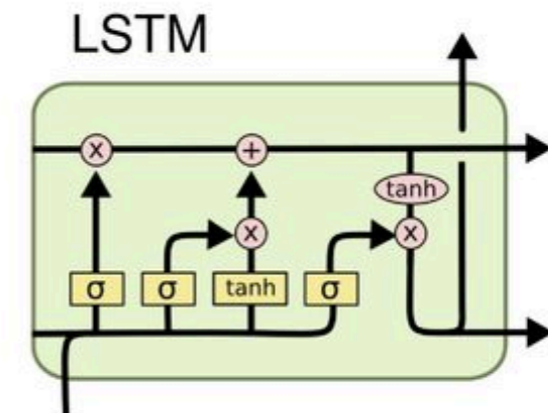
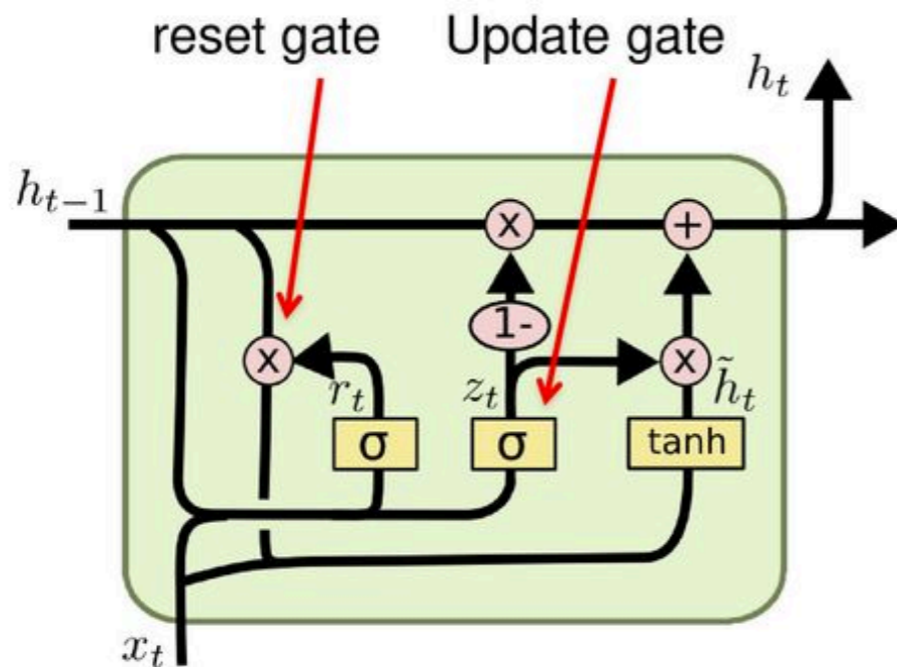
# Long Short Term Memory Networks





# Gated Recurrent Units (GRU)

## GRU – gated recurrent unit (more compression)



$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

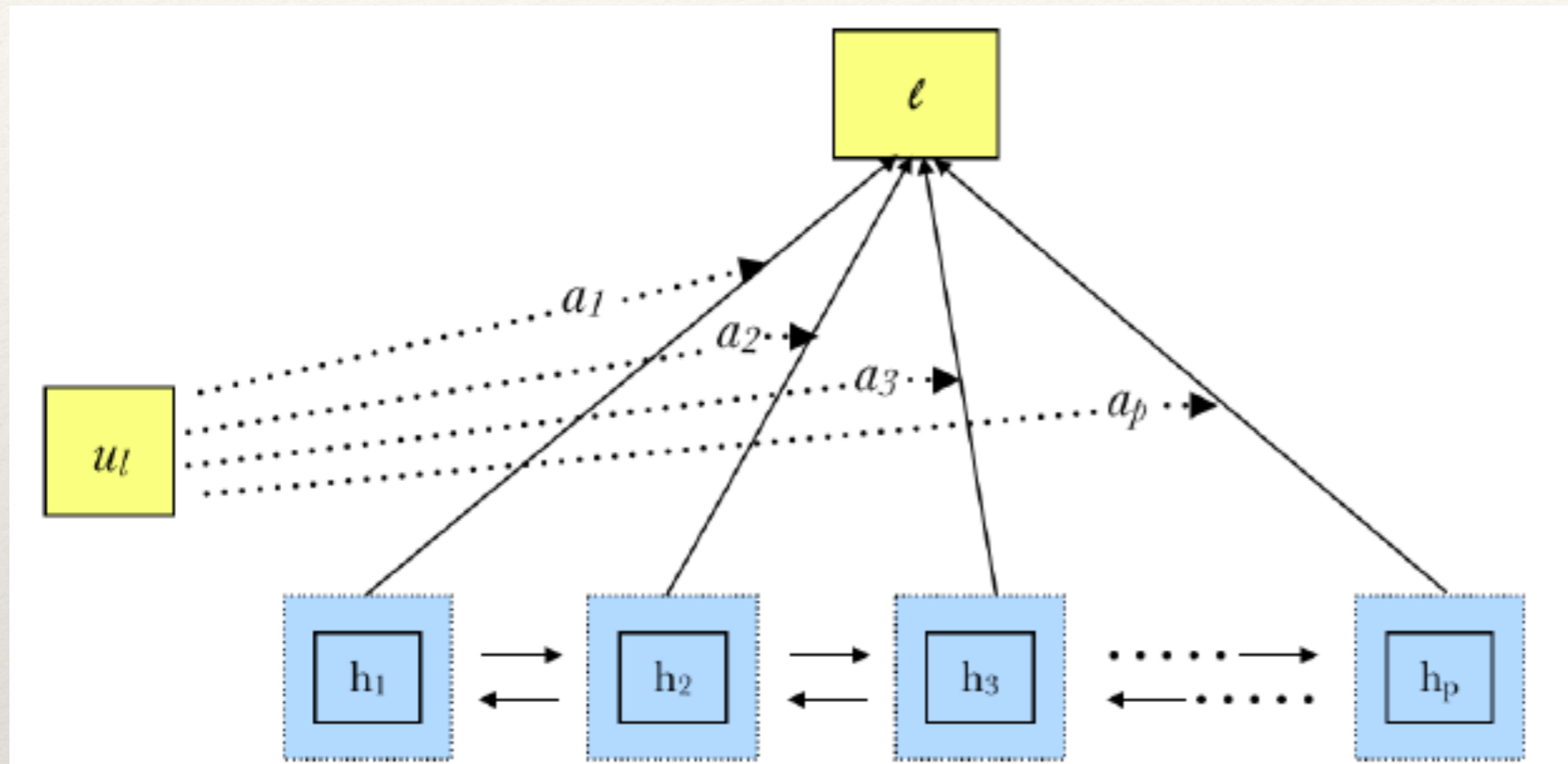
$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

It combines the **forget** and **input** into a single **update gate**.  
It also merges the cell state and hidden state. This is simpler than LSTM. There are many other variants too.

X,\*: element-wise multiply



# Attention in LSTM Networks



$$\mathbf{u}_t = \tanh(\mathbf{W}_l \mathbf{h}_t + \mathbf{b}_l)$$

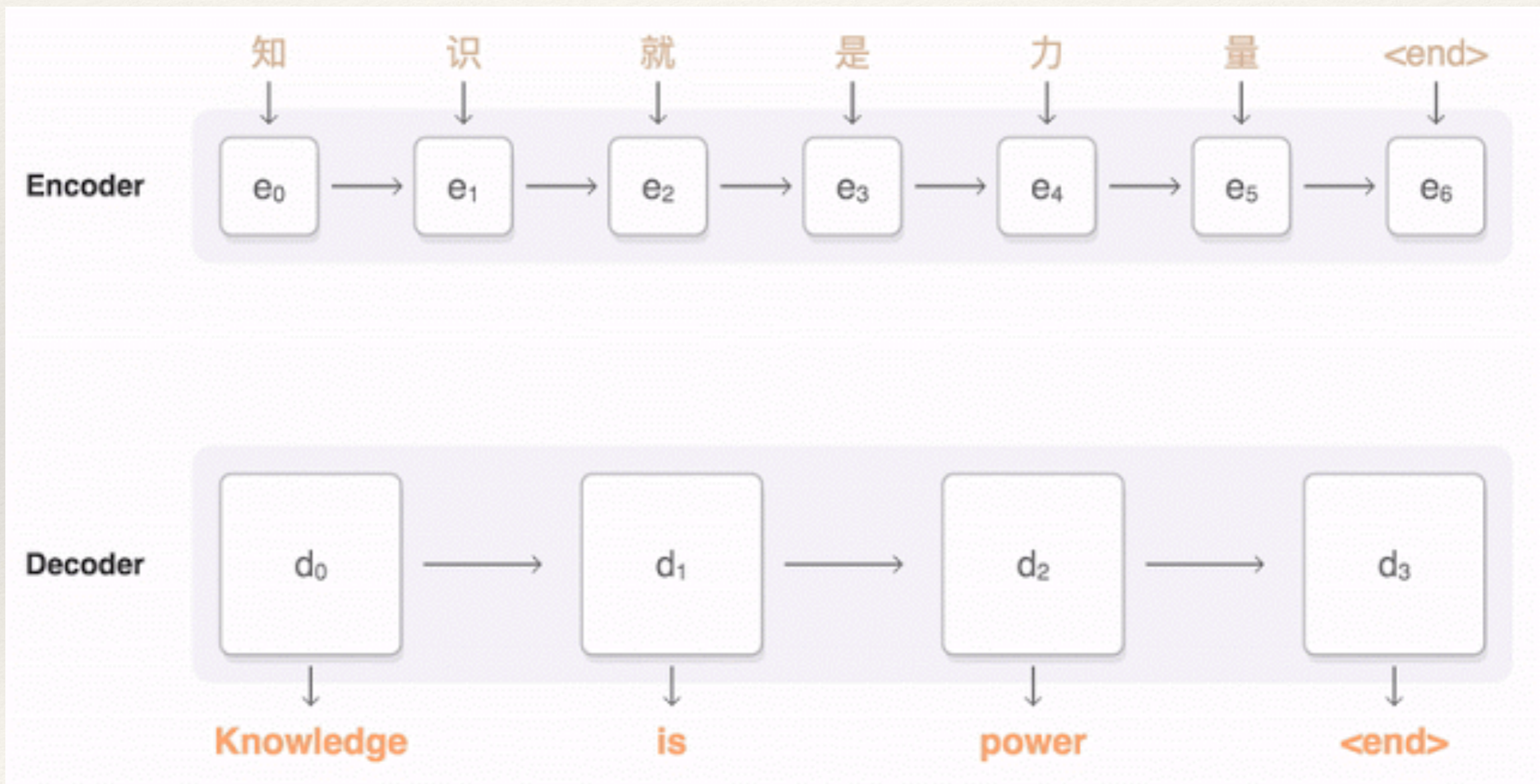
$$a_t = \frac{\exp(\mathbf{u}_t^T \mathbf{u}_l)}{\sum_t \exp(\mathbf{u}_t^T \mathbf{u}_l)}$$

$$\mathbf{l} = \sum_t a_t \mathbf{h}_t$$

- ❖ Attention allows a mechanism to add relevance
- ❖ Certain regions of the audio have more importance than the rest for the task at hand.



# Encoder - Decoder Networks with Attention









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# Attention - Speech Example

From our lab [part of ICASSP 2019 paper].



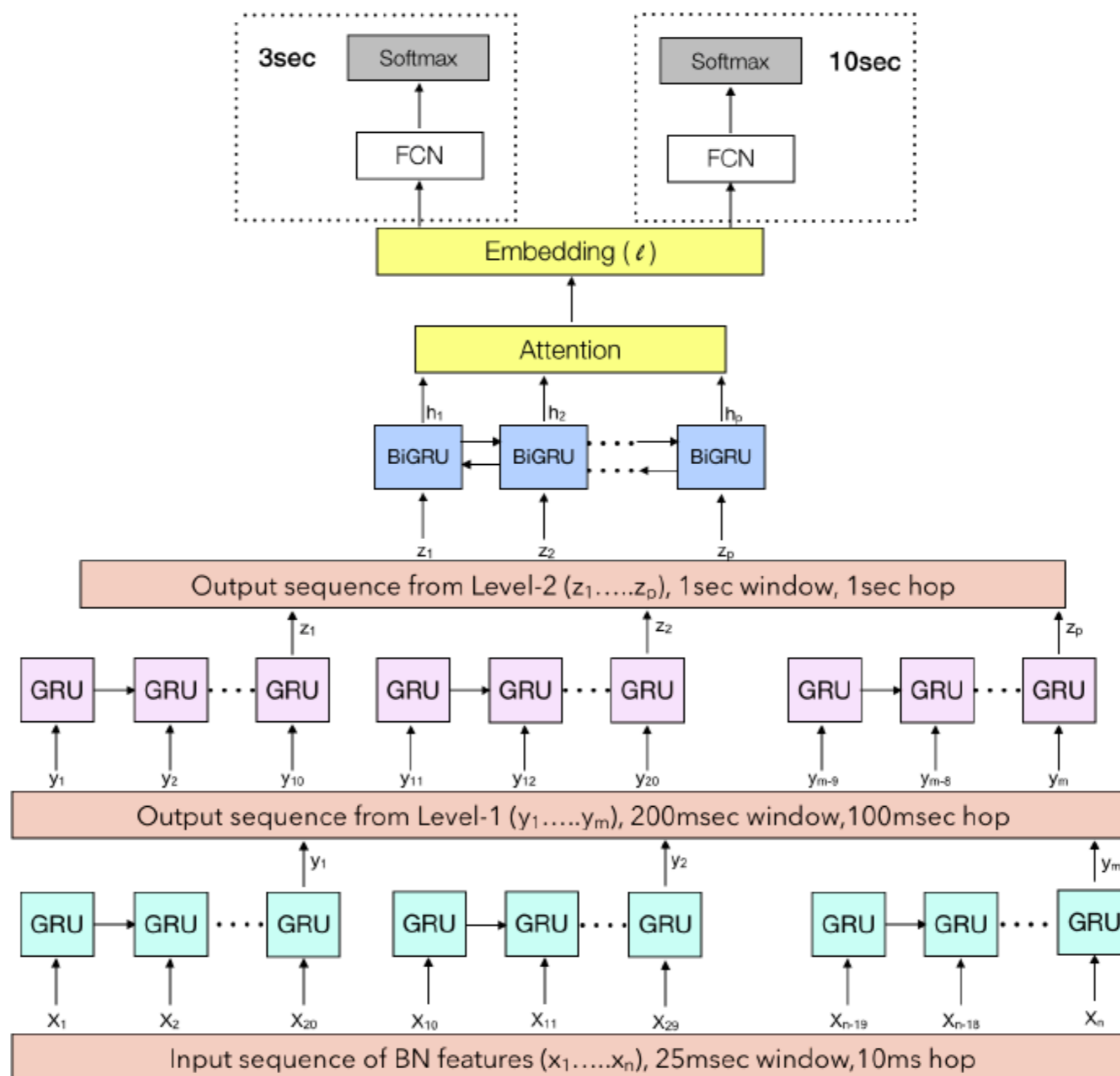
# Language Recognition Evaluation

Table 1: LRE17 training set : target languages, language clusters and total number of hours.

Cluster	Target Languages	Hours
Arabic	Egyptian Arabic (ara-arz)	190.9
	Iraqi Arabic (ara-acm)	130.8
	Levantine Arabic (ara-apc)	440.7
	Maghrebi Arabic (ara-ary)	81.8
Chinese	Mandarin (zho-cmn)	379.4
	Min Nan (zho-nan)	13.3
English	British English (eng-gbr)	4.8
	General American English (eng-usg)	327.7
Slavic	Polish (qsl-pol)	59.3
	Russian (qsl-rus)	69.5
Iberian	Caribbean Spanish (spa-car)	166.3
	European Spanish (spa-eur)	24.7
	Latin American Continental Spanish (spa-lac)	175.9
	Brazilian Portuguese (por-brz)	4.1

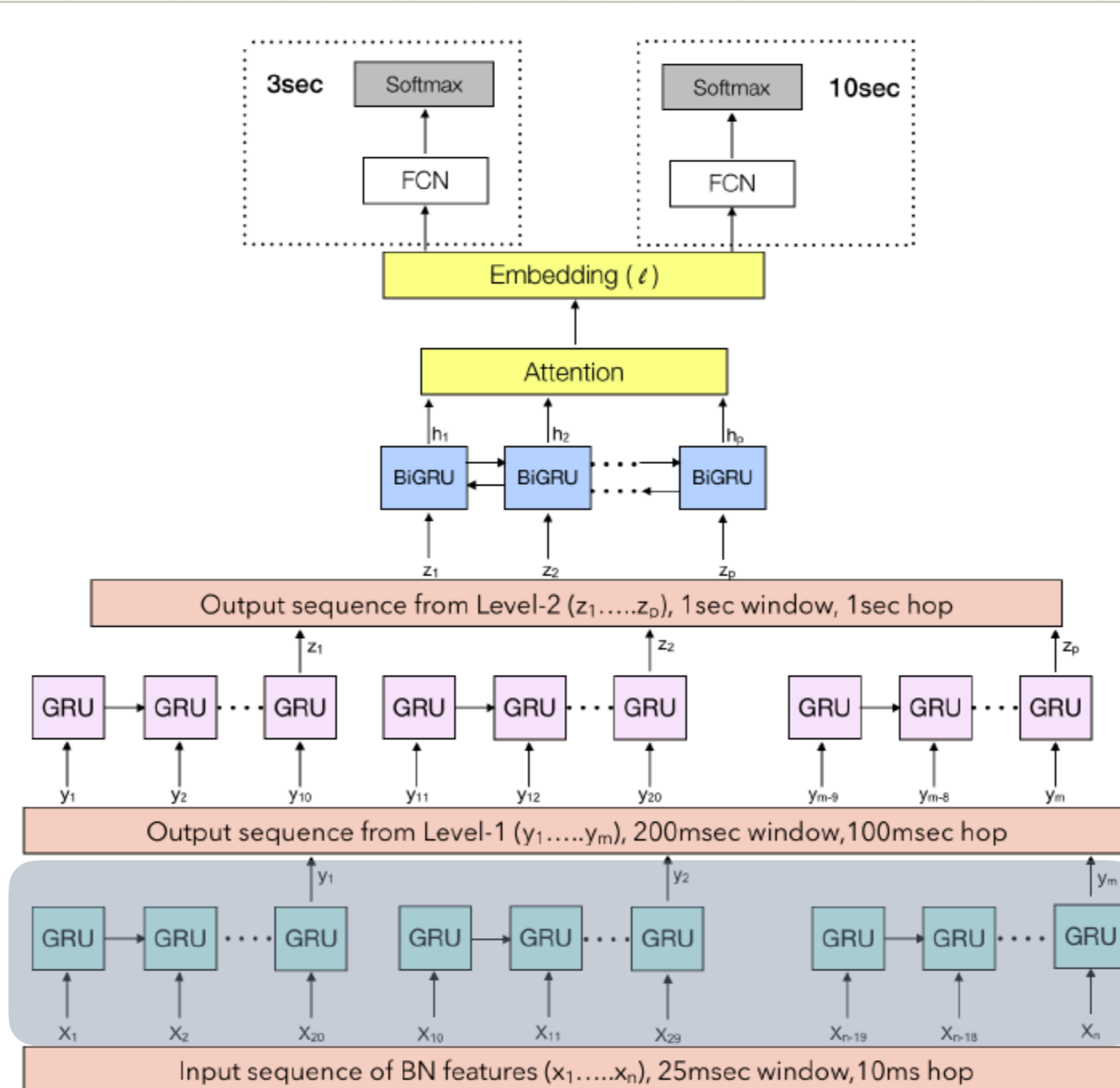


# End-to-end model using GRUs and Attention



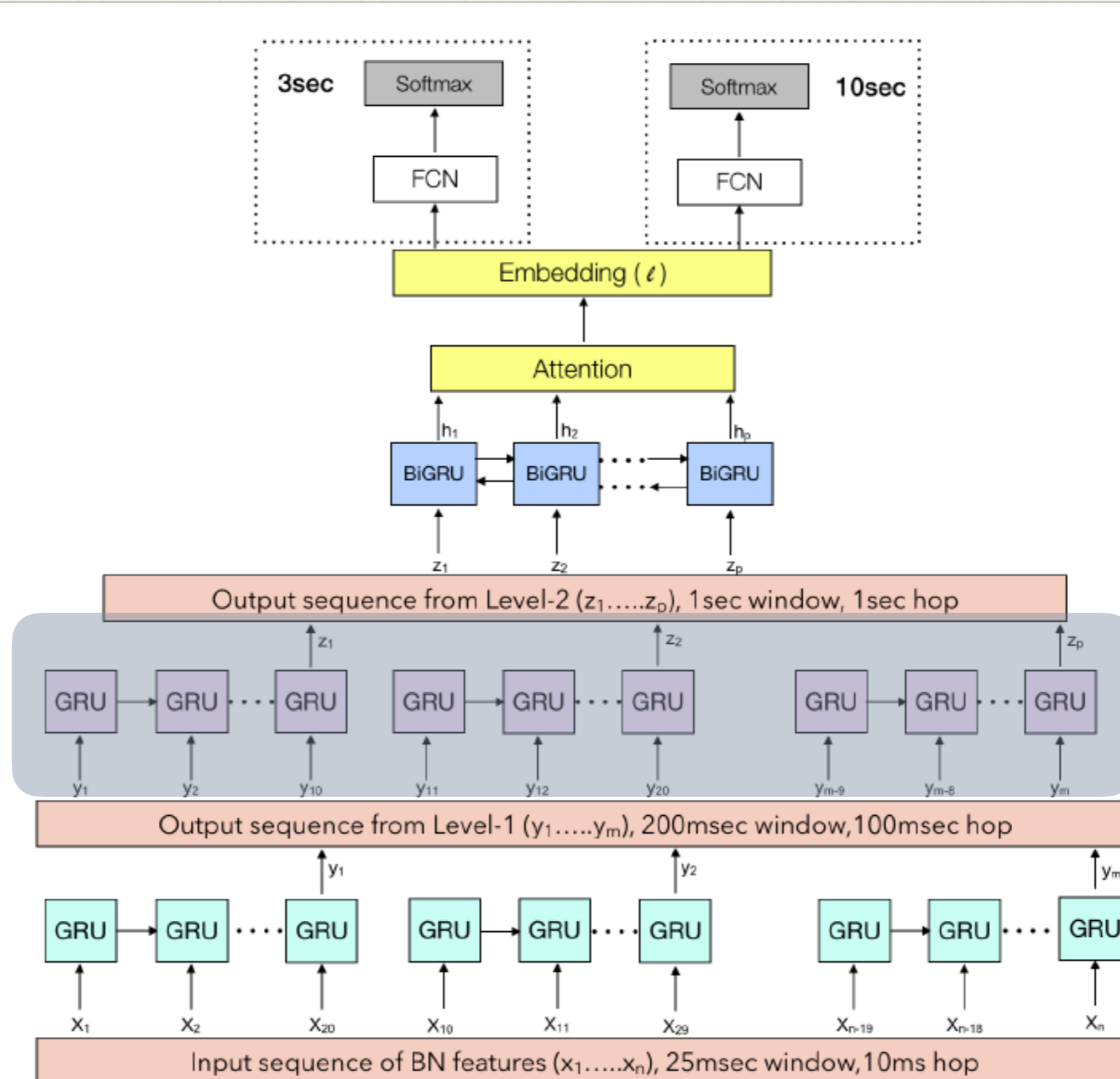


# Proposed End-to-End Language Recognition Model



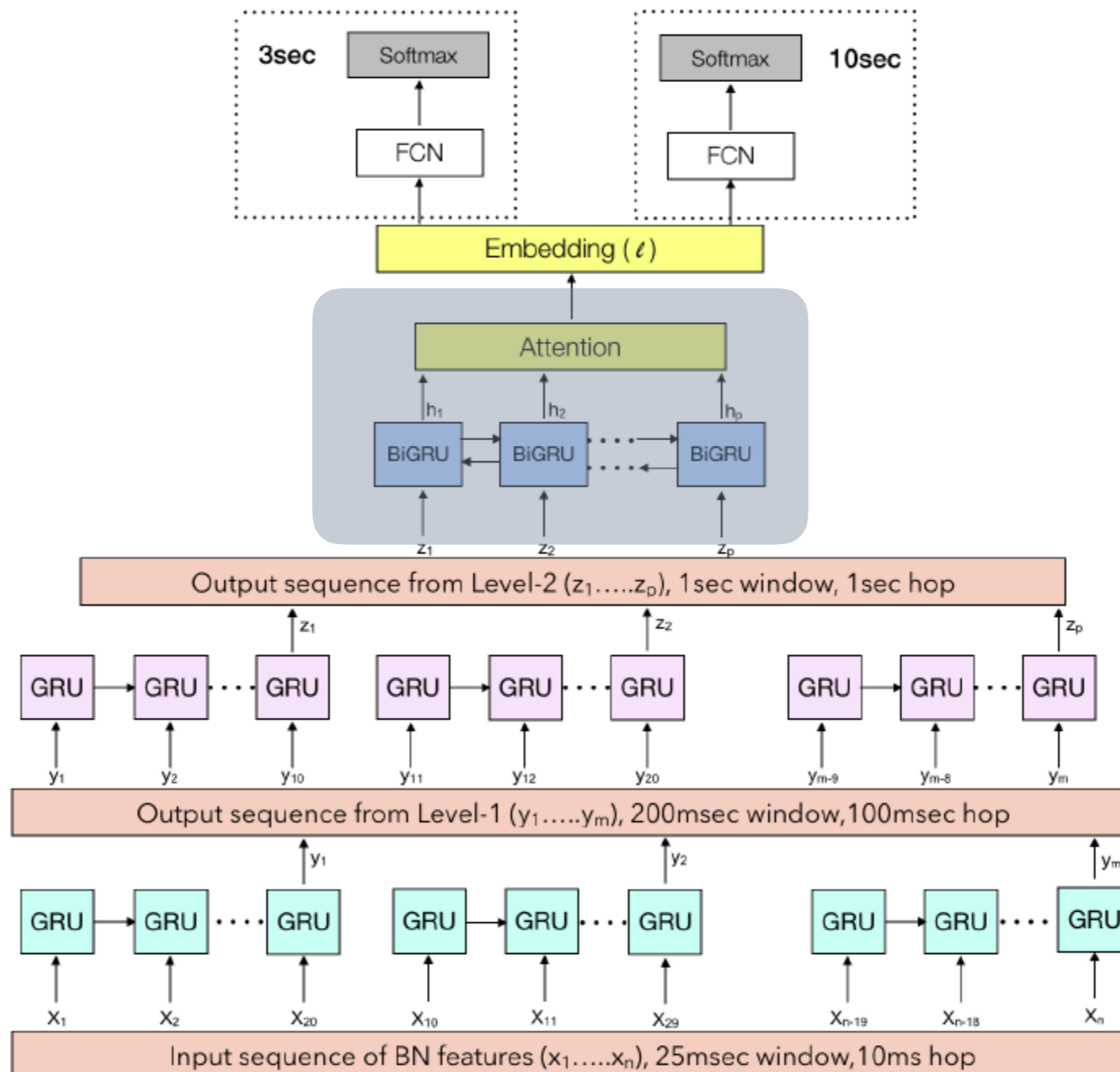


# Proposed End-to-End Language Recognition Model





# Proposed End-to-End Language Recognition Model





# Language Recognition Evaluation

- ❖ State-of-art models use the input sequence directly.
- ❖ We proposed the attention model - Attention weighs the importance of each short-term segment feature for the task.

## Attention Weight

0-3s : O...One muscle at all, it was terrible

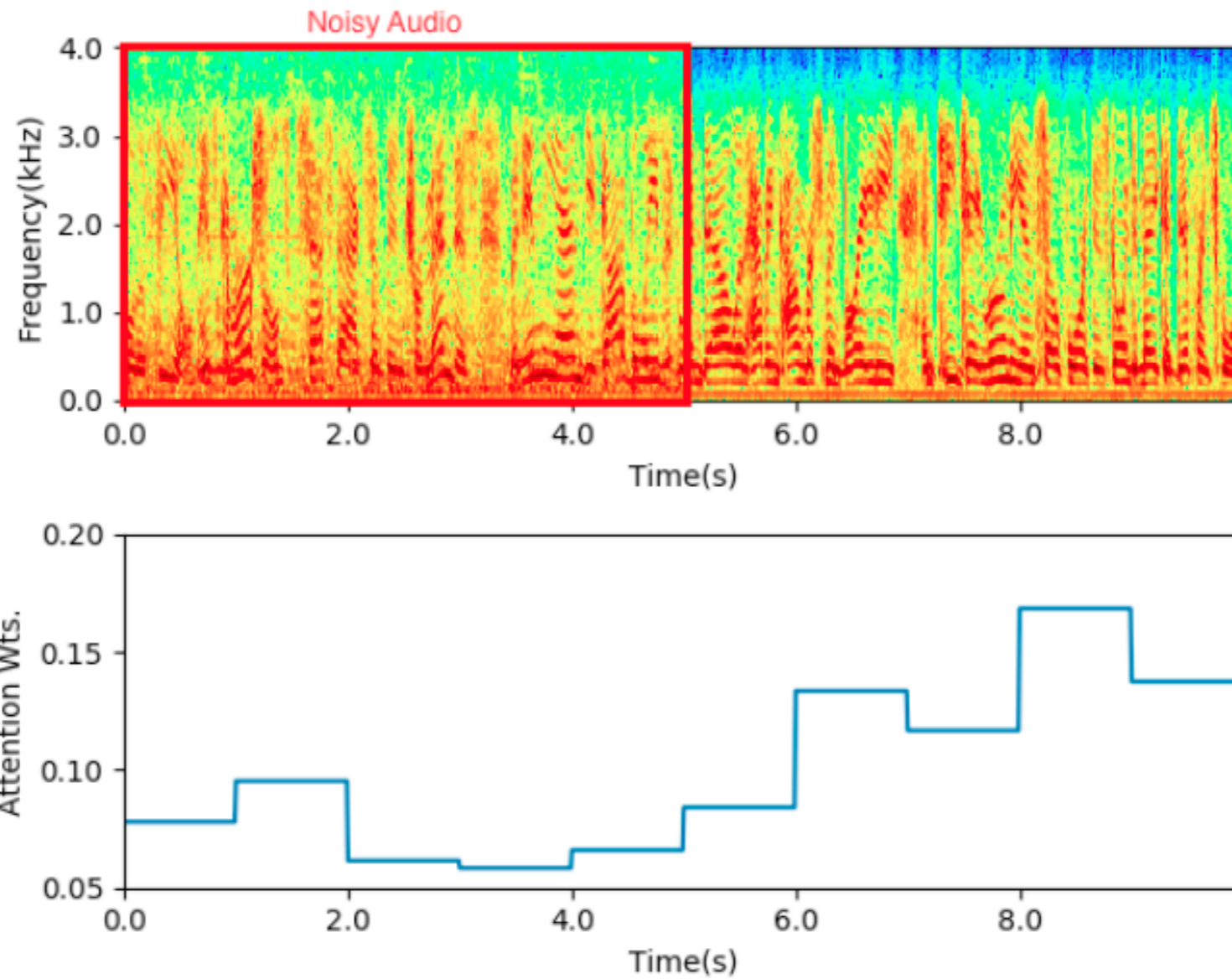
3s-4s : .... ah .... ah ....

4s - 9s : I couldn't scream, I couldn't shout, I couldn't even move my arms up, or my legs

9s -11s : I was trying me hardest, I was really really panicking.



# Language Recognition Evaluation





# Language Recognition Evaluation

**Table 3.** Approximate computational time in seconds for ten 30sec eval files using a single CPU. Machine Specification: 32 CPU, 8 core, 2 thread Intel x86\_64 machine with 16 GB Nvidia Quadro P5000 GPU cards.

	ivec. [19]	LSTM [16]	HGRU
CPU	12	51	8
GPU	12	11.5	1.5

**Table 4.** LID accuracy in % for additional experiments with multiple speakers speaking the same language and the experiments without any SAD information.

Cond.	i-vec. [19]	HGRU
Multi-Speaker	60.6	<b>67.7</b>
Without SAD information	49.7	<b>52.7</b>